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Application of the Extended Pairing Model to Heavy Isotopes

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Abstract. The binding energies of three isotopic chains ($^{100-130}\text{Sn}$, $^{152-181}\text{Yb}$, and $^{181-202}\text{Pb}$) are studied using the extended pairing model [1]. By using the exact solvability of the model one determines the pairing strength $G(A)$ that reproduces the experimental binding energies. For these isotopic chains, $\log(G(A))$ has a smooth systematic behavior. In particular, $G(A)$ for the Pb and Sn isotopes can be described by a two parameter expression that is inversely proportional to the dimensionality of the model space.

PACS. 21.10.Dr Binding energies – 71.10.Li Pairing interactions in model systems – 21.60.Cs Shell model

Exactly solvable models are essential in the understanding of various physics phenomena. For example, Elliott's SU(3) model provides a bridge between collective and microscopic single-particle shell-model description in nuclei. The pairing interaction is very important in nuclei and is also an exactly solvable. Recently, a whole new class of exactly solvable models, Richardson-Gaudin models, has been uncovered. Most of the current models, however, are mainly focused on Hamiltonians with two-body interactions, which is the currently accepted wisdom. For real applications, however, the infinite dimensional structure of the Hilbert space is a serious obstacle if the system under consideration is not exactly solvable or in a perturbative regime. In order to overcome this problem, one can construct an effective Hamiltonian in a finite model space. This, however, results in a many-body effective interaction terms. Never the less, the effective Hamiltonian approach has been applied with an increasing success, and even has pointed to the possible need of real three-body interactions in nuclei [2]. Therefore, the study of model Hamiltonians with many-body interactions would enhance our understanding of physical systems. The recently discovered exactly solvable many-body extended pairing model provides us with unique opportunity [1] for such a study. Its application to three isotope chains has shown that the model can be used for calculations of binding energies of heavy nuclei.

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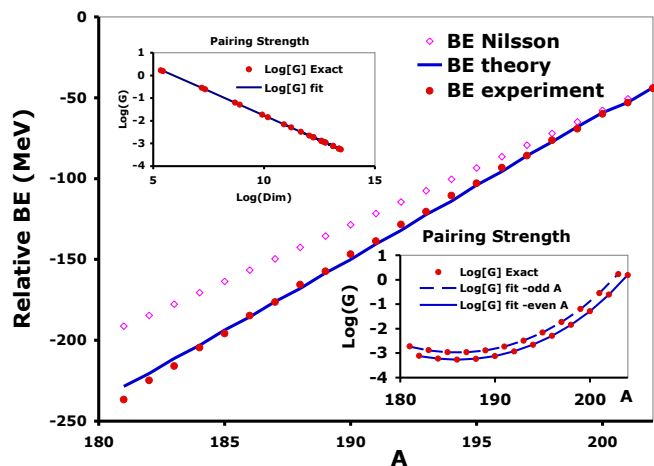


Fig. 1. The solid line gives the theoretical binding energy for the Pb isotopes relative to the ^{208}Pb nucleus. The insets show the fit to the values of G that reproduce exactly the experimental data using a ^{164}Pb core. The lower inset shows the two fitting functions: $\log(G(A)) = 382.3502 - 4.1375A + 0.0111A^2$ for even values of A and $\log(G(A)) = 391.6113 - 4.2374A + 0.0114A^2$ for odd values of A . The upper inset shows a fit to $G(A)$ that is inversely proportional to the size of the model space, $\text{dim}(A)$, that is valid for even as well as odd values of A : $G(A) = 366.7702/\text{dim}(A)^{0.9972}$. The Nilsson BE energy is the lowest energy of the non-interacting system.

References

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